# Sample Question Paper - 5 Mathematics-Standard (041) Class- X, Session: 2021-22 TERM II

# Time Allowed: 2 hours

## **General Instructions:**

- 1. The question paper consists of 14 questions divided into 3 sections A, B, C.
- 2. All questions are compulsory.
- 3. Section A comprises of 6 questions of 2 marks each. Internal choice has been provided in two questions.
- 4. Section B comprises of 4questions of 3 marks each. Internal choice has been provided in one question.
- 5. Section C comprises of 4 questions of 4 marks each. An internal choice has been provided in one question. It contains two case study-based questions.

### Section A

1. Find the 8<sup>th</sup> term from the end of the A.P. 7,10, 13, ..., 184.

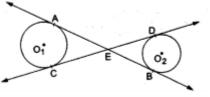
OR

Is the given series 2, 4, 8, 16, ..... form an AP? If It forms an AP, then find the common difference d and write the next three terms.

2. Solve the quadratic equation by factorization:

 $3x^2 - 14x - 5 = 0$ 

3. In the given figure, common tangents AB and CD to the two circles with centres  $O_1$  and  $O_2$  [2] intersect at E. Prove that AB = CD.



- 4. A copper sphere of radius 3 cm is melted and recast into a right circular cone of height 3 cm. [2] Find the radius of the base of the cone.
- 5. Write the frequency distribution table for the following data:

Marks(out of 90)	Number of candidates	
More than or equal to 80	4	
More than or equal to 70	6	
More than or equal to 60	11	
More than or equal to 50	17	

**Maximum Marks: 40** 

[2]

[2]

[2]

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More than or equal to 40	23
More than or equal to 30	27
More than or equal to 20	30
More than or equal to 10	32
More than or equal to 0	34

6. Find the roots of the quadratic equation  $4x^2 - 4px + (p^2 - q^2) = 0$ .

## OR

Find the roots of the quadratic equation given as:  $2x^2 + x - 4 = 0$  by applying the quadratic formula.

Section B

7. Find the mean, median and mode of the following data:

Class	0 - 20	20 - 40	40 - 60	60 - 80	80 - 100	100 - 120	120 - 140
Frequency	6	8	10	12	6	5	3

- 8. Construct a  $\Delta ABC$  in which AB = 5 cm.  $\angle B = 60^{\circ}$  altitude CD = 3 cm. Construct a  $\Delta AQR$  [3] similar to  $\Delta ABC$  such that side of  $\Delta AQR$  is 1.5 times that of the corresponding sides of  $\Delta ACB$ .
- 9. Find the mean of the following frequency distribution, using the assumed-mean method: [3]

Class	100 - 120	120 -140	140 - 160	160 - 180	180 - 200
Frequency	10	20	30	15	5

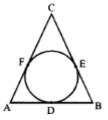
10. If a tower 30m high, casts a shadow  $10\sqrt{3}m$  long on the ground, then what is the angle of elevation of the sun?

OR

A man rowing a boat away from a lighthouse 150 m high takes 2 minutes to change the angle of elevation of the top of lighthouse from 45° to 30°. Find the speed of the boat. (Use  $\sqrt{3}$  = 1.732)

# Section C

- 11. An iron pillar has some part in the form of a right circular cylinder and remaining in the form [4] of a right circular cone. The radius of base of each of cone and cylinder is 8 cm. The cylindrical part is 240 cm high and the conical part is 36 cm high. Find the weight of the pillar, if one cubic cm of iron weighs 10 g.
- 12. In the adjoining figure, a circle inscribed in triangle ABC touches its sides AB, BC and AC at [4] points D, E and F respectively. If AB = 12 cm, BC = 8 cm and AC = 10 cm, find the lengths of AD, BE and CF.



OR

In the adjoining figure, a circle is inscribed in a quadrilateral ABCD in which  $\angle B$  = 90°. If AD = 23 cm, AB = 29 cm, and DS = 5 cm, find the radius (r) of the circle.

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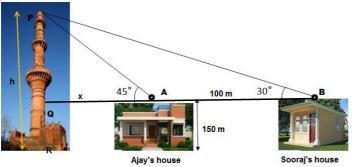
[2]

[3]

[3]

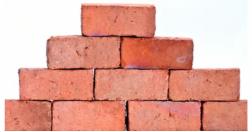


13. The houses of Ajay and Sooraj are at 100 m distance and the height of their houses is the same [4] as approx 150m. One big tower was situated near their house. Once both friends decided to measure the height of the tower. They measure the angle of elevation of the top of the tower from the roof of their houses. The angle of elevation of ajay's house to the tower and sooraj's house to the tower are 45° and 30° respectively as shown in the figure.



By using the above given information answer the following questions:

- i. Find the height of the tower.
- ii. What is the distance between the tower and the house of Sooraj?
- 14. Akshat's father is planning some construction work in his terrace area. He ordered 360 bricks [4] and instructed the supplier to keep the bricks in such as way that the bottom row has 30 bricks and next is one less than that and so on.



The supplier stacked these 360 bricks in the following manner, 30 bricks in the bottom row, 29 bricks in the next row, 28 bricks in the row next to it, and so on.

- i. In how many rows, 360 bricks are placed?
- ii. How many bricks are there in the top row?





#### Solution

### **MATHEMATICS STANDARD 041**

### **Class 10 - Mathematics**

### Section A

 A.P. 7, 10, 13,...., 184 Last term (l) = 184 Common difference(d) = 10 - 7 = 3 ∴ 8<sup>th</sup> term from end = 1 - (n - 1)d = 184 - (8 - 1) × 3 = 184 - 21 = 163

OR

If  $a_{k+1} - a_k$  is same for different values of k, then the series is in the form of an AP.

here, we have a<sub>1</sub> = 2, a<sub>2</sub> = 4, a<sub>3</sub> = 8 and a<sub>4</sub> = 16 a<sub>4</sub> - a<sub>3</sub> = 16 - 8 = 8

 $a_3 - a_2 = 8 - 4 = 4$  $a_2 - a_1 = 4 - 2 = 2$ 

Here,  $a_{k+1} - a_k$  i.e. the common difference is not same for all values of k

Hence, the given series does not form an AP.

2. We have,

 $3x^2 - 14x - 5 = 0$ So,  $3x^2 - 14x - 5 = 0$   $\Rightarrow 3x^2 - 15x + 1x - 5 = 0$   $\Rightarrow 3x(x - 5) + 1(x - 5) = 0$   $\Rightarrow (x - 5)(3x + 1) = 0$   $\Rightarrow x - 5 = 0 \text{ or } 3x + 1 = 0$  $\Rightarrow x = 5 \text{ or } x = -\frac{1}{3}$ . Hence the roots are 5 and  $-\frac{1}{3}$ 

3. We know that tangent segments to a circle from the same external point are congruent.

So, EA = EC for the circle having centre  $\mathsf{O}_1$ 

And, ED = EB for the circle having centre O<sub>2</sub>

Now, Adding ED on both sides in EA = EC, we get EA + ED = EC + ED  $\Rightarrow EA + EB = EC + ED$  $\Rightarrow AB = CD$ 

4. According to the question,we are given that, Radius of sphere = 3 cm Height of cone = 3 cm

Let, radius of cone = x cm According to question, we have,

Volume of sphere = Volume of cone

 $\Rightarrow \quad \frac{4}{3}\pi R^3 = \frac{1}{3}\pi r^2 h$   $\Rightarrow \quad \frac{4}{3} \times \frac{22}{7} \times 3 \times 3 \times 3 = \frac{1}{3} \times \frac{22}{7} \times x^2 \times 3$   $\Rightarrow \quad 4 \times 3 \times 3 \times 3 = x^2 \times 3$   $\Rightarrow \quad 36 = x^2$  $\Rightarrow \quad x = \sqrt{36} = 6 \text{ cm}$ 

Therefore, Radius of base of cone = 6 cm 5. **Frequency distribution table:** 

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Marks	Number of candidates
0 -10	34-32=2
10 - 20	32-30=2
20 - 30	30-27=3
30 - 40	27-23=4
40 - 50	23-17=6
50 - 60	17-11=6
60 - 70	11-6=5
70 - 80	6-4=2
more than 80	4

6. we have to find the roots of the quadratic equation  $4x^2 - 4px + (p^2 - q^2) = 0$ .

Here, a = 4, b = -4p,  $c = (p^2 - q^2)$ The roots are given by the quadratic formula  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$   $\therefore \quad x = \frac{4p \pm \sqrt{16p^2 - 4 \times 4 \times (p^2 - q^2)}}{2 \times 4}$   $= \frac{4p \pm \sqrt{16p^2 - 16p^2 + 16q^2}}{8}$   $= \frac{4p \pm 4q}{8}$ 

Therefore, the roots are  $rac{p+q}{2},rac{p-q}{2}$  .

OR

We have given that  $2x^2+x-4=0$ Comparing the given equation with standard form of quadratic equation  $ax^2 + bx + c$ we get, a = 2, b = 1, c = -4  $\therefore$  The roots are given as,  $\mathbf{x} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

$$= \frac{[-1\pm\sqrt{1-4(2)(-4)}]}{2\times 2} = \frac{-1\pm\sqrt{33}}{4}$$
  
:. The roots are  $\frac{-1+\sqrt{33}}{4}$  and  $\frac{-1-\sqrt{33}}{4}$ 

Section B							
Class interv	al Mid value (	x) Frequency (f	f) fx	Cumulative frequency			
0 - 20	10	6	60	6			
20 - 40	30	8	240	17			
40 - 60	50	10	500	24			
60 - 80	70	12	840	36			
80 - 100	90	6	540	42			
100 - 120	110	5	550	47			
120 - 140	130	3	390	50			
		N = 50	$\Sigma fx$ = 3120				
Mean $= \frac{\Sigma f x}{N} =$	$\frac{3120}{50} = 62.4$						

We have, N = 50

N = 50 Then,  $\frac{N}{2} = \frac{50}{2}$  = 25

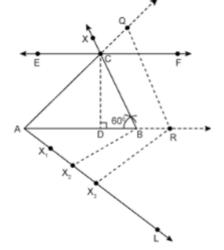
The cumulative frequency just greater than  $\frac{N}{2}$  is 36, then the median class is 60 - 80 such that l = 60, h = 80 - 60 = 20, f = 12, F = 24

Median = 1 + 
$$\frac{\frac{N}{2} - F}{f} \times h$$
  
= 60 +  $\frac{25 - 24}{12} \times 20$   
= 60 +  $\frac{20}{12}$   
= 60 + 1.67  
= 61.67

Here the maximum frequency is 12, then the corresponding class 60 - 80 is the modal class l = 60, h = 80 - 60 = 20, f = 12,  $f_1 = 10$ ,  $f_2 = 6$ 

Mode = 
$$l + \frac{f - f_1}{2f - f_1 - f_2} \times h$$
  
=  $60 + \frac{12 - 10}{2 \times 12 - 10 - 6} \times 20$   
=  $60 + \frac{40}{8}$   
=  $65$ 

8. Steps of construction:-



- i. Draw a line segment AB of length 5 cm.
- ii. Taking B as point construct an angle measure of  $60^\circ\mbox{using}$  a compass.
- iii. Name the angle as angle ABX.
- iv. Draw a line EF at a height of 3 cm such that it is parallel to the line segment AB. It must intersect ray BX at point C. Now join AC.
- v. Draw CD perpendicular to AB. CD is the altitude of riangle ABC having height 3 cm
- vi.  $\triangle$ AQR is 1.5 times that of the corresponding sides of  $\triangle$ ACB, i.e 3/2 times the corresponding sides of  $\triangle$ ACB.
- vii. Draw any ray AL making acute angle  $\angle BAL$  with AB.
- viii. Mark three points X<sub>1</sub>, X<sub>2</sub>, X<sub>3</sub> on AL.
  - ix. Join BX<sub>2</sub>, and draw line parallel to it passing from X<sub>3</sub>, intersecting AB extended at R.
  - x. Draw line parallel to CB through R to intersect AC extended at Q.
  - xi.  $\triangle ARQ$  is the required triangle.

Marks	Frequency(f <sub>i</sub> )	Mid value x <sub>i</sub>	d <sub>i</sub> = (x <sub>i</sub> - 150)	$(f_i  imes d_i)$
100 - 120	10	110	-40	-400
120- 140	20	130	-20	-400
140 - 160	30	150 = A	0	0
160 - 180	15	170	20	300
180 - 200	5	190	40	200

9. Let assumed mean (A) = 150.



$\Sigma f_i = 80$		$\Sigma\left(f_i imes d_i ight)=-300$
we know that ,		
$ ext{mean} = A + rac{\sum (f_i  imes d_i)}{\sum f_i}$		
$=\left(150+rac{(-300)}{80} ight)^{i}$		
= 150 - 3.75 = 146.25		
10. Let AB be the pole and let AC be its shadow.		
B Sun Sun C 10-/3 m A		
Let the angle of elevation of the sun be $\theta^{\circ}$ .		
Then, $igtriangle ACB= heta, igtriangle CAB=90^\circ.$ $AB=30m$ and AC = $10\sqrt{3}m.$		
From right $\Delta CAB$ , we have		
$ \tan \theta = \frac{AB}{AC} = \frac{30}{10\sqrt{3}} = \sqrt{3} $		
$\Rightarrow  heta = 60^{\circ}$		
	OR	

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Lighthouse 150 m

в

In right  $\triangle$  ABC,

 $= 54.9\ m/min$ 

AB = 150 m

30

Initially boat is at C and after 2 minutes it reaches at D.

С

2 minutes

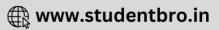
D

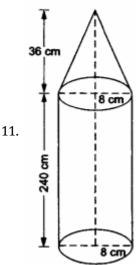
Distance covered in 2 minutes =  $BD - BC = 150\sqrt{3} - 150 = 150(\sqrt{3} - 1)m$   $\therefore$  speed =  $\frac{\text{Distance covered}}{\text{time taken}} = \frac{150(\sqrt{3} - 1)}{2}$ =  $75 \times (1.732 - 1)$ 

45'

 $\frac{AB}{BC} = \tan 45^{\circ}$   $\Rightarrow \frac{150}{BC} = 1 \Rightarrow BC = 150m$ In right  $\triangle ABD$ ,  $\frac{AB}{BD} = \tan 30^{\circ}$   $\Rightarrow \frac{150}{BD} = \frac{1}{\sqrt{3}} \Rightarrow BD = 150\sqrt{3}$ 

Section C





Let us suppose that r denotes the radius of the cylinder = 8 cm. Suppose R denotes the radius of the cone = 8 cm. Let h be the height of the cylinder = 240cm. Suppose H is the height of the cone = 36 cm. Total volume of the iron = volume of the cylinder + volume of the cone  $=\pi r^2h+rac{1}{3}\pi R^2H=\pi r^2\left(h+rac{1}{3}H
ight)$  [as r=R= 8cm each]  $=\left[rac{22}{7} imes 8 imes 8 imes \left(240+rac{1}{3} imes 36
ight)
ight]\mathrm{cm}^{3}$  $= 50688 \text{ cm}^3$  $\therefore$  Weight of the pilllar = volume in cm<sup>3</sup> imes weight per cm<sup>3</sup>  $= \left(\frac{50688 \times 10}{1000}\right) \mathrm{kg} = 506.88 \mathrm{kg}$ Therefore, the weight of the pillar is 506.88 kg. 12. We know that tangents drawn from an external point to a circle are equal.  $\Rightarrow$  AD = AF, BD = BE, CE = CF. Let AD = AF = a, BD = BE = b, CE = CF = cAB = AD + DB = a + b = 12 ------ (1) BC = BE + EC = b + c = 8 ------ (2) AC = AF + FC = a + b = 10 ----- (3) Adding (1), (2) and (3), we obtain 2(a + b + c) = 30 $\Rightarrow$  (a + b + c) = 15 ----- (4)

Subtracting (1) from (4), we get c = 3 Subtracting (2) from (4), we get a = 7 Subtracting (3) from (4), we get b = 5

Therefore, AD = a = 7 cm, BE = b = 5 cm and CE = 3 cm OR

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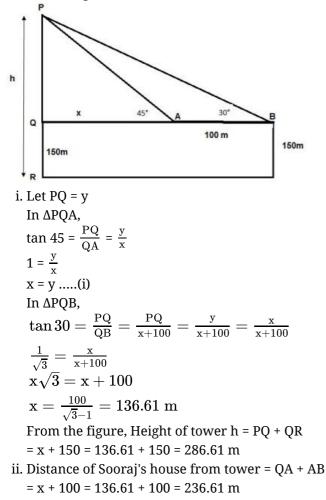
As we know that tangents drawn from an external point to a circle are equal, we can write DR = DS = 5 cm

$$A = \begin{bmatrix} Q \\ r \\ R \\ D \end{bmatrix} = \begin{bmatrix} P \\ r \\ r \end{bmatrix} = \begin{bmatrix} P \\ r \\ r \end{bmatrix} = \begin{bmatrix} P \\ r \\ r \end{bmatrix}$$

Therefore, we have, AR = AD - DR = 23 - 5 = 18 cm But, AR = AQ therefore, AQ = 18 cm and BQ = AB - AQ = 29 - 18 = 11 cm But, BP = BQ Therefore, BP = 11 cm Also,  $\angle Q = \angle P = 90^{\circ}$  (as tangents are perpendicular to radius at point of contact) In quadrilateral OQBP,  $\angle QOP + \angle P + \angle B + \angle OQB = 360^{\circ}$   $\angle QOB = 360^{\circ} - (\angle P + \angle Q + \angle B)$   $= 360^{\circ} - (90^{\circ} + 90^{\circ} + 90^{\circ}) = 90^{\circ}$ Hence, the given quadrilateral OQBP is a rectangle as all angles are 90°. Now, it's opposite sides would also be equal so, BQ = OP =11cm (BP = BQ = 11cm) and OQ = BP = 11 cm  $\therefore$  BQ = OQ = OP = BP = 11 cm As all sides are equal and all angles are of 90° Thus BQOP is a square.

Hence, the circle has the radius equal to 11 cm.

13. The above figure can be redrawn as shown below:



14. Number of bricks in the bottom row=30. in the next row=29, and so on.

therefore, Number of bricks stacked in each row form a sequence 30, 29, 28, 27,..., which is an AP with first term , a=30 and common difference, d=29 - 30 = -1.

Suppose number of rows is n, then sum of number of bricks in n rows should be 360 i.e.  $S_n = 360$  $\Rightarrow \frac{n}{2}[2 \times 30 + (n-1)(-1)] = 360 \{S_n = \frac{n}{2}(2a + (n-1)d)\}$  $\Rightarrow 720 = n(60 - n + 1)$ 

$$\Rightarrow 720 = n(60 - n + 1)$$

- $\Rightarrow 720 = 60$ n n<sup>2</sup> + n
- $\Rightarrow n^2 61n + 720 = 0$
- $\Rightarrow n^2 16n 45n + 720 = 0$  [by factorisation]
- $\Rightarrow n(n-16) 45(n-16) = 0$

$$\Rightarrow (n-16)(n-45)=0$$

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 $\Rightarrow (n - 16) = 0 \text{ or } (n - 45) = 0$   $\Rightarrow n = 16 \text{ or } n = 45$ Hence, number of rows is either 45 or 16. When, n = 16,  $a_{16} = 30 + (16 - 1)(-1) \{a_n = a + (n - 1)d\}$  = 30 - 15 = 15When, n = 45  $a_{45} = 30 + (45 - 1)(-1) \{a_n = a + (n - 1)d\}$ = 30 - 44 = -14 [:: The number of logs cannot be neagtive]

Hence, the number of rows is 16 and number of logs in the top row is 15.

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